planning 2022 lectures Reliability

Monday 14 november 2022

green = activing element

13:45-14:00 introduction SE Track Base by Dr. Ravenshorst

14:00-14:25 part 1 t/m part 4 (slide 1-28)

14:25-14:30 calculate reliability index β for given example (slide 29)

pauze

14:45-14:55 part 5 consequence classes (slide 30-34)

14:55-15:10 part 6 partial safety factors (slide 35-60)

15:20-15:30 part 7 combination factors (slide 61-73)

Thursday 17 november 2022

- 08:45-09:15 part 8 and 9 service life, ULS/SLS, load combinations (slide 74-78)
- 09:15-09:30 recap / in-class exercise with load combinations

09:45-10:30 Dr. Ajay Jagadeesh (pavement)

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- 2. STRUCTURAL SAFETY AND ACCEPTED RISKS
- 3. EUROCODE APPROACH
- 4. PROBABILITY OF FAILURE
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- 7. VARIABLE LOADS
- 8. DESIGN SERVICE LIFE
- 9. LIMIT STATES
- **10. LOAD COMBINATIONS**



Reliability Lecture 2.1.1 + 2.1.3a

Faculty of Civil Engineering and Geosciences MSc Civil Engineering

module: SE-TB-1 Sustainable Construction Members and Systems

Dr. Roel Schipper



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Learning objectives of these lectures

- Understand the concepts of reliability and apply these in practical verification of the safety
- Identify and quantify the most important loads on structures, roads and railway
- Schematise and combine them as input for the determination of the force distributions and deformations

(lecture 2.1.1 and 2.1.3a)

(lecture 2.7.1)

(lecture 2.7.3)



Assessment

- Formative (no grade) homework assignment on Load Analysis for a container port terminal
- Formative (no grade) homework assignment on Reliability
- Part of written exam (approx. 20 minutes)

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(week 2.1)
(week 2.7)
(week 2.10)
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Reference materials

- Lecture notes "Loads + Reliability", Module CIEM5000 – Structural Engineering Track Base, November 2022 (PDF, Brightspace: study this reader)
- Eurocodes

(online, for information and reference only)

 Quick Reference 2022 (PDF, Brightspace, for reference only)





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	cause	risk of dying (yearly)
voluntary risk	flying	$0.4 \cdot 10^{-6}$
	lethal accident while driving a bicycle	$13 \cdot 10^{-6}$
	lethal accident while driving a motorcycle	$5.5 \cdot 10^{-6}$
	drowning while swimming	$6.1 \cdot 10^{-6}$
	smoking	$1100 \cdot 10^{-6}$
involuntary risk	covid-19 (during 2020)	$1100 \cdot 10^{-6}$
	attack by an animal	$0.2 \cdot 10^{-6}$
	exposure to fire or smoke	$3.0 \cdot 10^{-6}$
	natural disaster, lightning, storm, floods	$0.03 \cdot 10^{-6}$
	gun violence	$1.5 \cdot 10^{-6}$

(number of yearly casualties in The Netherlands - risk is determined by number of cases divided by **total** population of approx. 17.6 million, CBS StatLine 2022)



"In The Netherlands, as a starting point it is assumed that the **risk from a hazardous activity** to a member of the public **should not add significantly** to the risk in every day life. The risk in every day life is taken as $P = 10^{-4}$, the **probability of death** for an unspecified individual person per year" (Ale, 1991)

"For **new hazardous installations** the maximum acceptable level for individual risk was set to $P = 10^{-6}$, which implicates an increase of the risk in every day life of 1%" (Ale, 1991)

"For **existing structures**, an individual risk of **P** = 10⁻⁵ for death of an individual person due to failure of a structural element is considered acceptable" (Vrouwenvelder and Scholten, 2008)



"For the risk of flooding, which can have massive consequences in terms of loss-of-life and economy, generally an individual risk limit between P = 10⁻⁵ and 10⁻⁶ was used for the design of hydraulic structures and dikes"

"In 2013 the Ministry of Infrastructure and the Environment proposed to use an individual risk P = 10⁻⁵. The Ministry explained that this choice was made because this risk is caused by nature, which is harder to influence than a manmade hazard. In addition, it was explained that a level of P = 10⁻⁶ for the entire area of the Netherlands would not be cost-effective"

(Terwel, 2014)









Figure 2.1: Fatality risk per 100 000 persons per year for different activities, related to degree of voluntariness and degree of influence on the risk (Schneider and Vrouwenvelder 2017)





Figure 2.2: Justifiable costs to prevent loss of life and limb. The monetary unit can be read as €, CHF, US\$, and £ in 2016, given the bandwidth / limited accuracy of the provided numbers (Schneider and Vrouwenvelder 2017)



Voluntary and involuntary risks - conclusions

Acceptable individual yearly risk as result of structural failure $\approx P_f = 10^{-5}$

At least four factors affect the accepted level of risk:

- 1. expected **consequences** of a failure
- 2. voluntariness of undergoing the risk
- 3. possibilities to **reduce** the risk
- 4. **cost-effectiveness** of reducing the risk



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Methods for the verification of adequate reliable performance of structures

-			
method	applied when		
Semi-probabilistic approach Safety	Default method in the Eurocodes, i.e. to		
format prescribing the design equations and the analysis procedures to be used	be used for usual design situations.		
Reliability-based design and assessment Reliability requirements to fulfil	Unusual design situations in regard to uncertainties, Code calibration.		
Risk-informed decision making Decisions are taken with due consideration of the total risks (e.g. loss of lives, injuries)	Exceptional design situations in regard to uncertainties and consequences. Derivation of reliability requirements.		



Risk-informed decision making

Exceptional design situations in regard touncertainties and consequences or derivation of reliability requirements.

example: storm surge barrier Oosterschelde





Reliability-based design and assessment

Unusual design situations in regard to uncertainties, code calibration

example: working in construction materials for which no code is available

Bamboo Bovenstad Rotterdam Pavilions





Reliability-based design and assessment

Unusual design situations in regard to uncertainties, code calibration

example: working in construction materials for which no code is available

Bamboo Bovenstad Rotterdam Pavilions





Reliability-based design and assessment

Applied to design situations where **uncertainties** in the representation of **loads**, load **effects**, **material** resistances, and **system-effects** mean that the reliability-based approach gives a significantly better representation of reality than the semi-probabilistic approach:

- situations where relevant loads or hazard scenarios are not covered by the loads and actions described in the code
- the use of building materials or combination of different materials outside the usual application domain
- new materials, behaviour at very high temperatures
- ground conditions, such as rock, which are strongly affected by discontinuities and other geometrical phenomena





Semi-probabilistic approach

Default method in the Eurocodes, i.e. to be used for usual design situations.





Methods for the verification of adequate reliable performance of structures

method	applied when
Semi-probabilistic approach Safety format prescribing the design equations and the analysis procedures to be used	Default method in the Eurocodes, i.e. to be used for usual design situations.
Reliability-based design and assessment Reliability requirements to fulfil	Unusual design situations in regard to uncertainties, Code calibration.
Risk-informed decision making Decisions are taken with due consideration of the total risks (e.g. loss of lives, injuries)	Exceptional design situations in regard to uncertainties and consequences. Derivation of reliability requirements.



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Probability of failure P_{f} and reliability index β

(pr	NEN-	EN-1990) 2021, t	able C.2))				
_	P_f	10^{-1}	10^{-2}	10^{-3}	10^{-4}	10^{-5}	10^{-6}	10^{-7}	10^{-8}
-	β	1.28	2.33	3.09	3.72	4.26	4.75	5.20	5.61

Table 2.3: Relation between failure probability P_f and reliability index β (prNEN-EN-1990 2021, table C.2)

Probability of failure P_f reliability index β





order of magnitude









https://gitlab.tudelft.nl/roelschipper/ciem5000/-/blob/main/Z_curve_highgamma_uc0.81_beta6.8.ipynb

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Table 2.5: Consequence classes for **buildings** Mind that National Annexes for CEN member states frequently define different combination values from the ones presented in these tables (draft prNEN-EN-1990 2021)

consequence class	description of consequence	examples for buildings		
CC3	higher	buildings where many people assemble, e.g. grandstands, concert and exposition halls, tall buildings, large public buildings		
CC2	normal	buildings where people normally enter, e.g. residential and office buildings, public buildings, industrial buildings with ≥3 layers		
CC1	lower	buildings where people do not normally enter, e.g. agricultural buildings, storage buildings, industrial buildings with 1 or 2 layers		

Table 2.6: Consequence	classes for	bridges	(draft	prNEN-EN-1990 2021)
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consequence class	description of consequence	examples for bridges		
CC3b	higher (upper risk group)	Where an increased level of reliability is required, when specified by the relevant authority or, where not specified, agreed for a specific project by the relevant parties		
CC3a	higher (lower risk group)	Railway bridges on main railway lines, bridges over main railway lines, bridges over and under major roads		
CC2	normal	Bridges not in other consequence classes		
CC1	lower	Short span bridges on local roads with little traffic (provided they do not span over main railway lines or major roads)		



indicative qualification 50-year reference period class consequences of consequences loss of economic, social or enhuman life or β_{50} $P_{f;50}$ personal vironmental injury consequences highest CC4 extreme huge $\sim 10^{-5} \\ \sim 10^{-4} \\ \sim 10^{-3}$ CC3 higher high 4.3 very great CC2 3.8 normal medium considerable CC1 3.3 low small lower CC0 very low insignificant lowest

Table 2.4: Consequence classes, qualification of consequences, reliability index β , probability of failure P_f , and consequence factor K_F in the Ultimate Limit State (prNEN-EN-1990 2021)



class	consequences	indicative qualification		1-year reference period	50-y	ear reference period
		of conse	of consequences			
		loss of human life or personal injury	economic, social or en- vironmental consequences	eta_1	eta_{50}	$P_{f;50}$
CC4	highest	extreme	huge			
CC3	higher	high	very great	5.2	4.3	$\sim 10^{-5}$
CC2	normal	medium	considerable	4.7	3.8	$\sim 10^{-4}$
CC1	lower	low	small	4.2	3.3	$\sim 10^{-3}$
CC0	lowest	very low	insignificant			

Table 2.4: Consequence classes, qualification of consequences, reliability index β , probability of failure P_f , and consequence factor K_F in the Ultimate Limit State (prNEN-EN-1990 2021)



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partial factors




effect of shift of σ_R (SD R) μ_R remains constant



















effect of shift of μ_R (mean R) σ_R remains constant

















effect of shift of μ_R (mean R) COV_R remains constant



















Partial factors for LOADS are in three main categories:

- **G** permanent loads (e.g. self weight, soil pressure, pretensioning) $\rightarrow \gamma_G$
- **Q** variable loads (e.g. wind, vehicles, people) $\rightarrow \gamma_Q$
- A accidental loads (e.g. blasts, impact, seismic) $\rightarrow \gamma_A$

limit state	design situation or load	СС	γ_G		γ_Q	γ_A
initi State	combination		un-	favour-		
			favour-	able		
			able			
persistent (perma	persistent (permanent) or	CC3	1.5	0.9	1.65	-
	transient (temporary) design situation (fundamental	CCS	1.3	0.9	1.65	-
		CC2	1.35	0.9	1.5	-
ultimate limit state (ULS)		CC2	1.2	0.9	1.5	-
		CC1	1.2	0.9	1.35	-
	combinations)	CCI	1.1	0.9	1.35	-
	accidental design	all	1.0	1.0	1.3	1.0
	situations					
	seismic design situations	all	1.0	1.0	1.0	1.0
serviceability limit	characteristic, frequent	all	1.0	1.0	1.0	-
state (SLS)	and semi-permanent					61
	design combinations					



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Table 2.12: Combination factors for road bridges

action	symbol		ψ_{0}	ψ_1	ψ_2
	gr1a (LM1 +	TS	0.75	0.75	0
	footway and	UDL	0.40	0.40	0
traffic loads (coo	cycle-track loads)	Footway+cycle-	0.40	0.40	0
NEN EN 1001 2 table		track loads			
6 E and 6 6	gr1b (single axle)		0	0.75	0
0.5 and 0.0)	gr2 (horizontal forces)		0	0	0
	gr3 (pedestrian loads)		0	0.40	0
	gr4 (LM4 - crowd load	ing)	0	-	0
	gr5 (LM3 - special		0	-	0
	vehicles)				
wind forces	$F_{W,k}$ persistent		0.6	0.2	0
	$F_{W,k}$ execution		0.8	-	0
	F_W		1.0	-	-
thermal actions	T_m		0.6	0.6	0.5
snow loads	$Q_{sn,k}$		0	0	0
water actions				i	72
construction actions	Q_c		1.0	-	1.0

nex)			
action	ψ_0	ψ_1	ψ_2
imposed loads in buildings:			
Category A: domestic, residential areas	0.7 (0.5)	0.5	0.3
Category B: office areas	0.7 (0.5)	0.5	0.3
Category C: congregation areas	0.7 (0.25)	0.7	0.6
Category D: shopping areas	0.7 (0.4)	0.7	0.6
Category E: storage areas	1.0	0.9	0.8
Category F: traffic area, vehicle weight $\leq 30 \text{ kN}$	0.7	0.7	0.6
Category G: traffic area, $30 \mathrm{kN}$ vehicle weight $\leq 160 \mathrm{kN}$	0.7	0.5	0.3
Category H: roofs accessible for normal maintenance and repair	0.7 (0)	0.2 (0)	0
only			
Construction loads: see NEN-EN-1991-1-6 (2005)	0.6 to 1.0	-	0.2
Snow loads on buildings			
- Finland, Iceland, Norway, Sweden	0.7	0.5	0.2
 Remainder of CEN member states, for sites located at altitude H 	0.7	0.5	0.2
> 1000 m			
 Remainder of CEN member states, for sites located at altitude H 	0.5 (0)	0.2	0
\leq 1000 m			
Wind loads in buildings: see NEN-EN-1991-1-4 (2005)	0.6 (0)	0.2	0
Temperature (non-fire) in buildings: see NEN-EN-1991-1-5 (2005)	0.6 (0)	0.5	0
Icing: see EN 1991-1-9	0.5	0.2	0
Standing water	-	-	-
Waves and currents: see EN 1991-1-8	-	-	-

Table 2.11: Combination factors for buildings (values in parentheses are from Dutch National An-

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Design service life

Table 2.9. Design service me for bundings (draft priveri-1990 2021)			
category of buildings	design service life $T_{\sf life}$ [years]		
monumental building structures	100		
building structures not covered by any	50		
other category			
agricultural, industrial, and similar	25		
structures	23		
temporary structures ^{a,b}	≤ 10		
	•		

Table 2.9: Design service life for buildings (draft prNEN-EN-1990 2021)

Table 2.10: Design service life for bridges (draft prNEN-EN-1990 2021)

category of bridges	design service life T_{life} [years]
bridges (including their foundations and tension	100^{b}
components), other civil engineering structures	
supporting road or railway traffic ^a	
bridges where the main structural members have	50 ^b
reduced protection ^a	
replacable structural parts other than tension	25
components	
temporary structures ^c	≤ 10
	category of bridges bridges (including their foundations and tension components), other civil engineering structures supporting road or railway traffic ^a bridges where the main structural members have reduced protection ^a replacable structural parts other than tension components temporary structures ^c

Design service life – load correction

$$F_t = F_{t;0} \left(1 + \frac{1 - \psi_0}{9} \ln \frac{T_{\text{life;chosen}}}{T_{\text{life;required}}} \right)$$
(2.9)

In which:

 F_T the adjusted characteristic value of the variable load to be used for the adjusted design service life $F_{T;0}$ the characteristic value of the variable load for a design service life $T_{\text{life}} = 50$ years ψ_0 combination factor, see below $T_{\text{life;chosen}}$ adjusted design service life (may be either shorter or longer than $T_{\text{life;required}}$) $T_{\text{life;required}}$ design service life $T_{\text{life;required}} = 50$ years



Design service life – load correction



In which:

 $\begin{array}{ll} F_T & \mbox{the adjusted characteristic value of the variable load to be used for the adjusted design service life} \\ F_{T;0} & \mbox{the characteristic value of the variable load for a design service life} \\ T_{\rm life; chosen} & \mbox{combination factor, see below} \\ T_{\rm life; required} & \mbox{design service life (may be either shorter or longer than } T_{\rm life; required}) \\ T_{\rm life; required} & \mbox{design service life } T_{\rm life; required} = 50 \ {\rm years} \end{array}$

Adjustment of characteristic value of variable loads for adjusted design service life

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Ultimate Limit State (ULS)

If **failure or collapse** is at risk, we call this limit state the Ultimate Limit State (or ULS).

An ULS often is an irreversible state that leads to significant and permanent damage or even collapse, concerning safety of the structure itself or the people using it.

Examples are loss of equilibrium, instability, material yield due to excess stress or fatigue.





Ultimate Limit State (ULS)

If **failure or collapse** is at risk, we call this limit state the Ultimate Limit State (or ULS).

An ULS often is an irreversible state that leads to **significant and permanent damage or even collapse**, concerning **safety of the structure itself** or the **people** using it.

Examples are loss of equilibrium, instability, material yield due to excess stress or fatigue.





Example ULS: collapse stadium grand stand

video NEC-stadium




Serviceability Limit State (SLS)

The Serviceability Limit State (or SLS) is reached when **deformations**, **vibrations or deflections** are becoming so large that proper functioning (**service**) of the structure is no longer possible

or when **comfort of occupants** is at risk, although the structural reliability is not (yet) at stake.

Beyond SLS, the structure is no longer able to perform its **service or the durability** of the structure might be at risk (e.g. crack width in concrete becomes too large, or corrosion occurs).

Also **architectural damage** (e.g. discolouring, cracks, problems with airtightness) is often considered as SLS.

An SLS may in many cases be a **reversible state**, that can be made undone after the load has reduced again.

However, it can also be considered as **irreversible damage** which is not of major and direct significance for the structure's structural reliability (you might think of small cracks in walls or permanent deformation as a result of creep). Repair or maintenance is considered an acceptable way of mitigating the effects of passing the SLS-threshold.





Example SLS check: Zalmhaventoren Rotterdam (guest lecture BAM) modal shape analysis - torsional acceleration and displacements



Case	Mode	Period	Freq	UX	UY	Sum UX	Sum UY	RZ	Sum RZ
		sec	Hz				100000		100510
Modal	1	4.10	0.24	0.53	0.04	0.53	0.04	0.00	0.00
Modal	2	4.05	0.25	0.04	0.53	0.57	0.57	0.00	0.00
Modal	3	1.94	0.51	0.00	0.00	0.57	0.57	0.00	0.56
Modal	4	0.77	1.30	0.00	0.21	0.57	0.78	0.00	0.00
Modal	5	0.76	1.32	0.20	0.00	0.77	0.78	0.00	0.00
Modal	6	0.59	1.71	0.00	0.00	0.77	0.78	0.00	0.20

Case	Mode	Period	Freq	UX	UY	Sum UX	Sum UY	RZ	Sum
		Sec	Hz						
Modal	1	4.56	0.22	0.53	0.04	0.53	0.04	0.00	0.00
Modal	2	4.52	0.22	0.03	0.53	0.56	0.56	0.00	0.00
Modal	3	2.21	0.45	0.00	0.00	0.56	0.56	0.55	0.55
Modal	4	0.89	1.12	0.00	0.20	0.56	0.76	0.00	0.55
Modal	5	0.88	1.13	0.19	0.00	0.76	0.76	0.00	0.55
Modal	6	0.66	1.52	0.00	0.00	0.76	0.76	0.19	0.74

Tabel 10. Eigenfrequenties in gescheurde toestand UGT.



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Load combinations

ULS:
$$\sum_{j\geq 1} \gamma_{G,j} \mathsf{G}_{k,j} + \gamma_P \mathsf{P} + \gamma_{Q,i=1} \mathsf{Q}_{k,i=1} + \sum_{i>1} \gamma_{Q,i} \psi_{0,i} \mathsf{Q}_{k,i}$$
(2.10)

- G_k, P, Q_k characteristic values for permanent, prestress and variable loads (for prestress $P_k = P$)
- $\begin{array}{lll} \gamma_G, \ \gamma_P, \ \gamma_Q & \mbox{partial load factors for permanent, prestress and variable loads } (\gamma_G \ \mbox{and } \gamma_Q \ \mbox{from Table 2.7 on page 19, } \gamma_P \ \mbox{from material codes}) \\ j & \mbox{index counting permanent loads } (1 \ \mbox{or more}) \\ i = 1 & \mbox{index counting the first variable load as dominant} \\ i > 1 & \mbox{index counting remaining variable loads as non-dominant} \\ \psi_{o,i} & \mbox{combination value for all remaining variable loads with index count } i > 1 \\ + & \mbox{to be read as: "to be combined with". Could be either a positive or negative} \\ & \mbox{value, depending on which of the two results in the worst load for the structure.} \end{array}$



(2.10)

choose one variable load as the dominant variable load (numbered i=1)

ULS: $\sum_{i\geq 1} \gamma_{G,j} \mathsf{G}_{k,j} + \gamma_P \mathsf{P} + \left(\gamma_{Q,i=1} \mathsf{Q}_{k,i=1}\right) + \sum_{i\geq 1} \gamma_{Q,i} \psi_{0,i} \mathsf{Q}_{k,i}$

choose all other variable loads (numbered i = 2, ..., n) as non-dominant by using **combination factor** ψ_0

repeat this procedure by alternating all variable loads as governing ones until you find the load combination that results in the worst effect on the structure

this will generally result in **MANY** combinations!

and it can be **tricky** to find out **if** a combination is governing.



Load combinations

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RECAP



